explained if their molar volume were to coincide with the smallest extreme of their lattice parameter uncertainty (4.462  $\pm$  0.002 Å vs. the x-ray value of 4.4638 Å).<sup>7</sup> The agreement with the theoretical calculation is good above 7 K for the n = 12 model, although the volume dependence of  $C_V$  as calculated on this model is not correct.<sup>30</sup> The difficulty most likely lies in the form of the two-body potential which was used for these calculations, and there are prospects for better potentials in the near future.<sup>5</sup>

The comparison in Fig. 7 of the present results and the values of  $\Theta$  which are derived from  $C_P$  data is not very satisfactory since the earlier data have been processed in two ways. First, the smoothed values of  $C_P$  have been converted to  $C_V$  using

$$C_P = C_V (1 + \beta \gamma T) \tag{8}$$

where  $\gamma$  is given by Eq. (5), and second, the values of  $C_V$  for each temperature have been adjusted to make them correspond to the 0 K equilibrium volume. The present results suggest a simple model for solid neon in which  $C_V$  is a function only of the reduced temperature  $T/\Theta_0(V)$ . Hence, the known thermal expansion for solid neon<sup>7</sup> can be used to determine the molar volume and  $\Theta_0$  at P = 0 for each temperature, after which  $C_V$  can be obtained from the reduced curve. In practice, the relationships of Figs. 5 and 6 are used together with a tabulation of the Debye function. The values of  $\Theta_0$  which result from the use of the equation-of-state expression for  $\gamma_0$  ( $\gamma_0 = 0.197 \pm 0.002$  cm<sup>-3</sup>. V) range from 75.1 K at  $V_0 = 13.391$  cm<sup>3</sup>/mole to 66.8  $\pm$  0.5 K at the triple point (24.6 K, 14.02 cm<sup>3</sup>/mole), where  $T/\Theta_0 = 0.37$ . The use of a constant value  $\gamma_0 = 2.51$  would not alter these results appreciably.  $C_P$  then is calculated from Eq. (8), using Eq. (5) to calculate  $\gamma$  and the x-ray values<sup>7</sup> for the thermal expansion coefficient  $\beta$ .

The resulting relationship for  $C_P(T, P = 0)$  is given as the solid line in Fig. 8, where it is compared with direct determinations of  $C_P$ .<sup>11,12,17</sup> The



Fig. 8. A comparison of  $C_P$  as calculated from the present results and as obtained from the smoothed results of Refs. 11 (FH), 12 (FS), and 17 (Clusius).

agreement below 20 K is well within the experimental uncertainties, especially if the data of Clusius *et al.*<sup>17</sup> (taken for the pure isotope <sup>20</sup>Ne, T > 8 K) are increased slightly to compensate for the 1% isotopic mass difference between their sample and natural neon. Above 20 K, the smoothed results of Fenichel and Serin<sup>12</sup> begin to deviate systematically from the other data, as do the data of Fagerstroem and Hollis-Hallet<sup>11</sup> above 23 K. The latter authors give only a plot for this temperature region, and the points in Fig. 8 were read from the smooth curve in this plot. If the values of  $\gamma$  which are used in Eq. (8) to calculate  $C_P$  from our model for  $C_V$  are calculated from experimental thermodynamic quantities<sup>7-9</sup> in a self-consistent fashion instead of using our equation of state, the predicted curve for  $C_P$  would tend to bend over above 21 K to a value of roughly 24 J/mole-K at the triple point.

The agreement for  $C_p$  between the relation which is calculated from our  $C_V$  data and the results of Clusius *et al.*<sup>17</sup> is excellent at all temperatures, as is the agreement with Fagerstroem and Hollis-Hallet<sup>11</sup> at 23 K and below. The reason for the rapid increase in  $C_p$ , which both Fenichel and Serin<sup>12</sup> and Fagerstroem and Hollis-Hallet<sup>11</sup> observe near the melting point, is not clear. None of our samples show a premelting anomaly of this magnitude (see Fig. 4, for instance, where the melting temperature is 46.8 K, and Fig. 6), in basic agreement with the results of Clusius *et al.*<sup>17</sup> Schoknecht and Simmons<sup>31</sup> have shown recently that vacancy effects should be quite small in  $C_p$  for solid neon near these temperatures. Our calculated values of  $C_p$  also are in excellent agreement with those given by Goldman *et al.*<sup>2</sup> for their m = 12 ISC calculation.

The present data can be used to test the Lindeman melting relation which associates the melting temperature  $T_m$  with the relative mean square amplitude  $x^2 = \langle \delta r^2 \rangle / r_s^2$ ,  $(4\pi r_s^3/3) = V_m$  of the atomic vibrations in the solid at the melting line. The usual relation<sup>33</sup>

$$x^{2} = (9\hbar^{2}/mk_{B})(T_{m}/\Theta^{2}r_{s}^{2}) = 41.11 \,(\text{cm}^{2}\cdot\text{K})(T_{m}/\Theta^{2}V_{m}^{2/3})$$
(9)

(where  $\hbar$  and  $k_B$  are the Planck and Boltzmann constants, respectively, and m is the mass of the atom) is applicable only for  $T_m > \Theta$ , whereas the melting temperatures of solid neon in Table I all are less than  $0.6\Theta_0$ . Hence, we have calculated a Debye model generalization of Eq. (9) following Ziman's approach,<sup>32</sup> in which  $x^2$  becomes [with  $x^2_{\text{classical}}$  given by Eq. (9)]

$$x^{2} = x_{\text{classical}}^{2} [1 + (z^{2}/36) - (z^{4}/3600) + (z^{6}/2.12 \times 10^{5}) - \cdots]$$
(10)

where  $z = \Theta/T_m$ . This expression is valid for the present range of z and is based on a series expansion<sup>33</sup> of the integrand of Ziman's equation (2.111).<sup>32</sup>

Figure 9 gives a plot of x as calculated from the present data (Table I) for both Eqs. (9) and (10), with  $\Theta = \Theta_0$ . This plot is given in terms of  $T_m/\Theta_0$